

SECTION A (40 MARKS)
ANSWER ALL QUESTIONS

Mark

Direction: For each question, there are FOUR responses: A, B, C, and D. Choose the corresponding letter of your response and CIRCLE it neatly. NO score will be awarded if you circle more than ONE letter.

[40]

i. Two matrices can be added if

- A both have same order.
- B both are rectangular matrices.
- C number of columns in the first matrix is equal to number of rows in the second matrix.
- D number of rows in the first matrix is equal to number of columns in the second matrix.

2

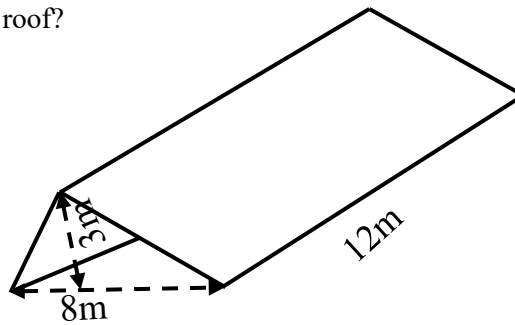
Answer: **A both have same order.**

Criteria	Marks
Circles the correct option	2
Circles more than ONE alternative	0
Circles none of the alternatives	0

2

ii. Yeashi plans to replace the wooden roof of his house with metal sheets as it is more durable. How much metal sheet is required to cover the roof?

- A $36 m^2$
- B $60 m^2$
- C $120 m^2$
- D $240 m^2$



2

Answer: $Width\ of\ a\ rectangular\ face = \sqrt{(4)^2 + (3)^2} = \sqrt{25}$
 $= 5\ m$

$The\ amount\ of\ metal\ roof\ required = 2(12m \times 5m)$
 $= 120m^2$

iii. If Pelden borrowed Nu 30,000 and repaid the loan with a single payment of Nu 37,960 at the end of 3 years, with interest compounded semi-annually, the rate of interest would be

- A 4%.
- B 8%.
- C 9%.
- D 12%.

2

Answer: 8%

Given :principal = Nu30,000. Amount = 37,960. Time = 3yrs. $n = 2$. Rate = ?

$$A = P \left(1 + \frac{r}{n} \right)^{nt}$$

$$37,960 = 30,000 \left(1 + \frac{r}{2} \right)^{2 \times 3}$$

$$\frac{37,960}{30,000} = \left(1 + \frac{r}{2} \right)^6$$

$$1.2653 = \left(1 + \frac{r}{2} \right)^6$$

$$\sqrt[6]{1.2653} = 1 + \frac{r}{2}$$

$$1.0400 = 1 + \frac{r}{2}$$

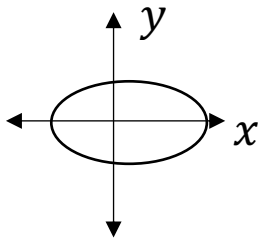
$$1.0400 - 1 = \frac{r}{2}$$

$$0.0400 = \frac{r}{2}$$

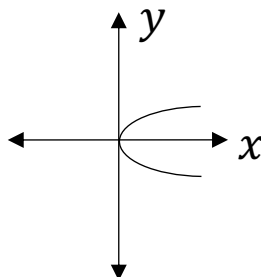
$$r = 8\%$$

iv. Which of the following graph represents function?

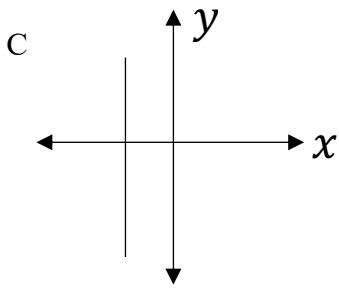
A



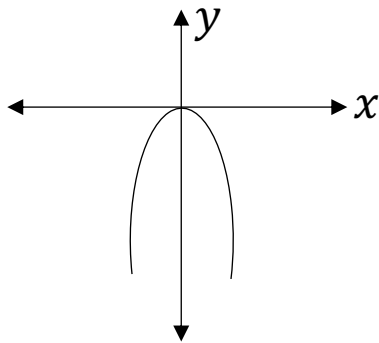
B



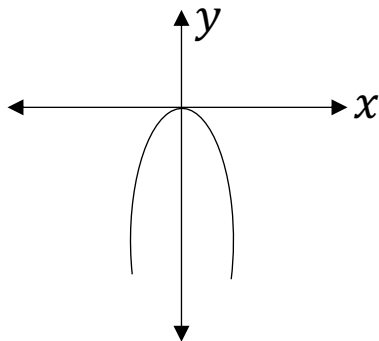
2



(D)



Answer: D



2

v. There are three paths through a triangular park. Each path goes from the midpoint of one edge to the opposite corner and the paths meet at point P. The point P is known as

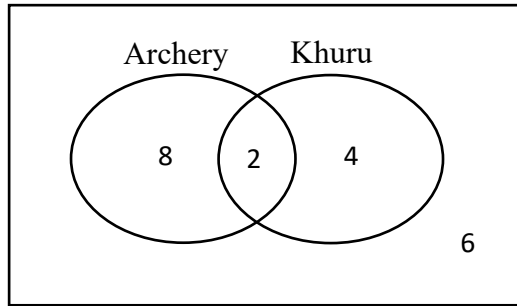
- A median.
- B altitude.
- (C) centroid.
- D orthocenter.

2

Answer: C centroid

2

vi. The Venn diagram shows the number of students who like to play indigenous games.



If a student is randomly selected, what is the probability that the student who likes to play archery is selected?

[2]

A $\frac{4}{20}$

B $\frac{6}{20}$

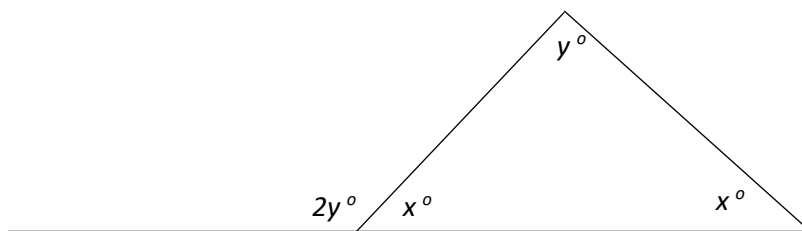
C $\frac{8}{20}$

D $\frac{10}{20}$

Answer : $\frac{8}{20} + \frac{2}{20} = \frac{10}{20}$

2

vii. The value of y in the given diagram is



2

A 36° .

B 60° .

C 108° .

D 120° .

Answer: 60°

$$2x + y = 180^\circ \text{ -----eq i}$$

$$x + 2y = 180^\circ \text{ -----eq ii}$$

$$2(2x + y = 180^\circ)$$

Subtracting (equ i) from (equ iii)

$$4x + 2y = 360 \text{ -----eq iii}$$

$$x + 2y = 180 \text{ -----eq i}$$

$$3x = 180$$

$$x = \frac{180}{3} = 60^\circ$$

Substituting value of x in (equ i)

$$60 + 2y = 180$$

$$2y = 180 - 60$$

$$2y = 120$$

$$y = \frac{120}{2} = 60^\circ$$

viii. If $\cot \theta = \frac{4}{3}$, which lies in the first quadrant, what is the value of $\operatorname{cosec} \theta$?

A $-\frac{5}{3}$

B $-\frac{3}{5}$

C $\frac{3}{5}$

D $\frac{5}{3}$

Answer : D $\frac{5}{3}$

$$\cot \theta = \frac{4}{3} = \frac{A}{O}$$

$$H^2 = 4^2 + 3^2 \rightarrow H^2 = 25$$

$$H = 5$$

$$\operatorname{Cosec} \theta = \frac{H}{O} = \pm \frac{5}{3}$$

Since: θ lies in first quadrant, $\therefore \operatorname{Cosec} \theta = \frac{5}{3}$

2

ix. The number of reflectional symmetry in the given figure is

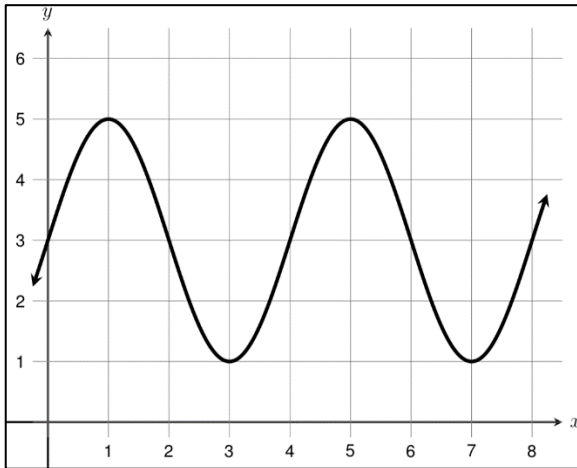
- A 2.
- B 4.
- C 8.
- D 10.



[2]

Answer : C 8

x. Which of the following relation will result in the curve below?



- A edge of a cube and its volume
- B side length of a rectangle and its area
- C time and height of a person on the seesaw
- D time and height of a cannon ball shot in the air

[2]

Answer : C Time and height of a person the seesaw.

xi. Simplify the expression: $\sqrt{8y} + 5\sqrt{50y} - 2\sqrt{18y}$

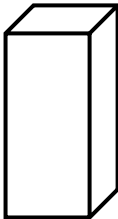
- A $13\sqrt{2y}$
- B $21\sqrt{2y}$
- C $294y$
- D $(8 + 5\sqrt{50} - 2\sqrt{18})y$

[2]

<p>Answer: B $21\sqrt{2y}$</p> $\sqrt{8y} + 5\sqrt{50y} - 2\sqrt{18y}$ $2\sqrt{2y} + 5 \times 5\sqrt{2y} - 2 \times 3\sqrt{2y}$ $2\sqrt{2y} + 25\sqrt{2y} - 6\sqrt{2y}$ $(2 + 25 - 6)\sqrt{2y}$ $21\sqrt{2y}$	
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<p>xii. Which of the following equation matches the pair of roots -3 and 9?</p> <p><input checked="" type="radio"/> A $x^2 - 6x - 27 = 0$</p> <p><input type="radio"/> B $x^2 - 12x - 27 = 0$</p> <p><input type="radio"/> C $x^2 - 12x - 9 = 0$</p> <p><input type="radio"/> D $x^2 - 6x - 9 = 0$</p>	[2]
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<p>Answer : $x^2 - 6x - 27 = 0$</p> $(x + 3)(x - 9) = 0$ $x^2 - 9x + 3x - 27 = 0$ $x^2 - 6x - 27 = 0$	
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<p>xiii. A square based rectangular block of wood was cut into eight equal cubes with edges of 4 cm. Find the volume of the initial rectangular block of wood.</p> <p><input type="radio"/> A 64 cm^3</p> <p><input type="radio"/> B 128 cm^3</p> <p><input type="radio"/> C 256 cm^3</p> <p><input checked="" type="radio"/> D 512 cm^3</p>		[2]
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<p>Answer: D 512 cm^3</p> <p><i>volume of a cube</i> $= s^3$</p> $= 4^3$ $= 64\text{ cm}^3$ <p><i>volume of 8 such cubes</i> $= 8 \times 64$</p> $= 512\text{ cm}^3$	
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xiv. 'y' as a function of 'x' in the equation $2x + 3y = 5$ is

A $f(x) = \frac{5-2x}{3}$.

B $f(x) = \frac{5-3y}{2}$.

C $f(y) = \frac{5-2x}{3}$.

D $f(y) = \frac{5-3y}{2}$.

[2]

Answer: A $f(x) = \frac{5-2x}{3}$

xv. If A and B are two matrices of order $3 \times p$ and $3 \times q$ respectively and $p = q$ then the order of the matrix $\left(\frac{1}{2}A - 2B\right)$ is

A $q \times 3$

B $p \times 3$

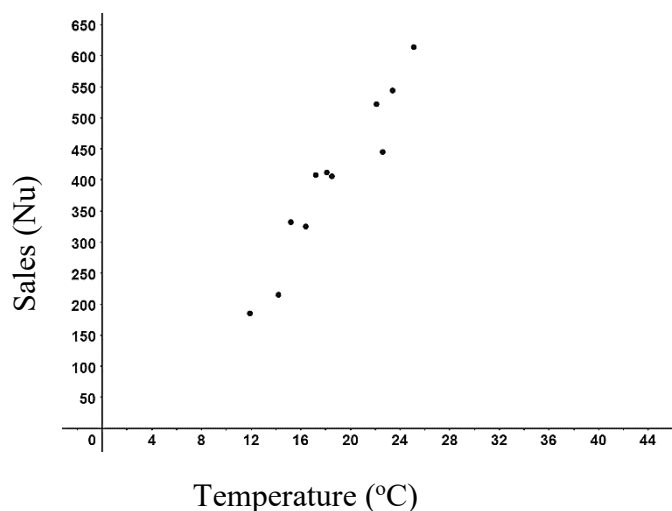
C $3 \times p$

D $p \times q$

[2]

Answer : C $3 \times p$

xvi. The scatter plot shows the record of ice cream sale versus the noon temperature. What type of correlation coefficient does the given scatter plot show?



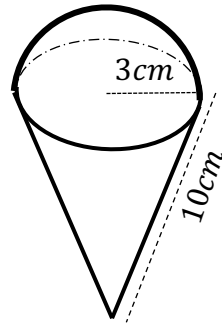
[2]

- A -1
- B 1
- C Close to -1
- D Close to 1

Answer : D close to 1

xvii. The total surface area of the given shape is

- A 94.3 cm^2 .
- B 150.8 cm^2 .
- C 179.1 cm^2 .
- D 207.4 cm^2 .



[2]

Answer: B 150.8 cm^2

$$SA = SA_{\text{cone}} + SA_{\text{hemisphere}}$$

$$SA = \pi r s + 2\pi r^2$$

$$SA = [\pi \times 3 \times 10] + [2\pi \times (3)^2]$$

$$SA = 94.25 + 56.55$$

$$SA = 150.8 \text{ cm}^2$$

xviii. Which of the following functions are equivalent?

$$f(x) = 2x^2 + 4x - 6 \quad g(x) = 2(x-1)(x+3) \quad h(x) = 2(x+1)^2 - 3$$

- A $f(x)$ and $g(x)$
- B $f(x)$ and $h(x)$
- C $g(x)$ and $h(x)$
- D $f(x)$, $g(x)$ and $h(x)$

[2]

Answer: A $f(x)$ and $g(x)$

$$g(x) = 2(x-1)(x+3)$$

$$g(x) = (2x-2)(x+3)$$

$$g(x) = (2x^2 + 6x - 2x - 6)$$

$$g(x) = 2x^2 + 4x - 6$$

$$h(x) = 2(x+1)^2 - 3$$

$$h(x) = 2(x^2 + 2x + 1) - 3$$

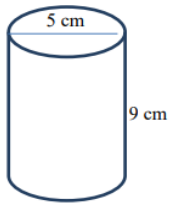
$$h(x) = 2x^2 + 4x + 2 - 3$$

$$h(x) = 2x^2 + 4x - 1$$

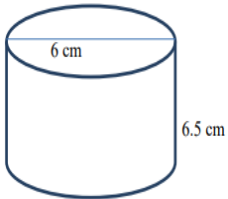
Hence $f(x)$ and $g(x)$ are equivalent

xix. Four cylinders have the same total surface area but different dimensions. Which is the most efficient cylinder?

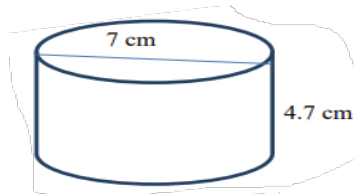
A



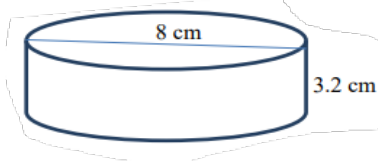
B



C

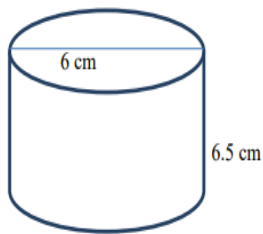


D



[2]

Answer B



Since the diameter and the height of the cylinder are almost equal.

xx. Evaluate the value of: $\sec 30^\circ \tan 60^\circ + \sin 45^\circ \operatorname{cosec} 45^\circ + \cos 30^\circ \cot 60^\circ$.

A $\frac{\sqrt{2}}{\sqrt{3}}$

B $\frac{11}{6}$

C $\frac{16}{6}$

D $\frac{7}{2}$

[2]

Answer D $\frac{7}{2}$

$$\frac{2}{\sqrt{3}} \times \sqrt{3} + \frac{1}{\sqrt{2}} \times \sqrt{2} + \frac{\sqrt{3}}{2} \times \frac{1}{\sqrt{3}}$$
$$= 2 + 1 + \frac{1}{2}$$
$$= \frac{7}{2}$$

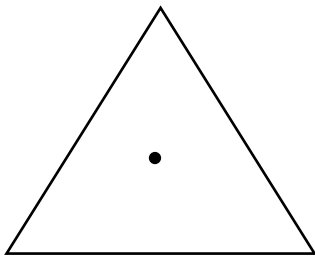
SECTION B (60 MARKS)
ANSWER ANY SIX QUESTIONS

Question 2

a) Create a 2-D shape with turn symmetry of the following order and locate its centre of rotation.

i. 3

[2]

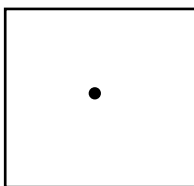


Correct shape with 3 order of turn symmetry. -----[1]

Correct location of centre of rotation. -----[1]

ii. 4

[2]

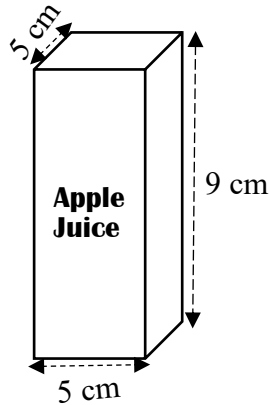
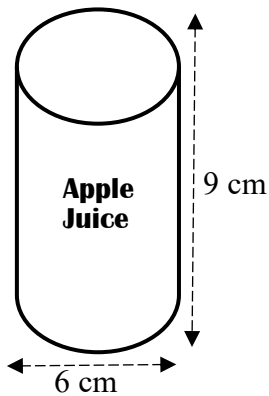


Correct shape with 4 order of turn symmetry. -----[1]

Correct location of centre of rotation. -----[1]

b) As Sangay is preparing for a hike, he intends to buy juice from a shop. The shop offers two different packaging options for the same type of juice: one in a can and the other in a tetra pack as shown in the figure. Both packaging have the same price.

[3]



Which

juice pack should Sangay buy? Justify.

Given :

$$r = 3 \text{ cm} \quad h = 9 \text{ cm}$$

Volume of a cylinder = $\pi r^2 h$

$$= \pi (3)^2 \times 9 \text{ -----} [0.5]$$

$$= 254.47 \text{ cm}^3 \text{ ----} [0.5]$$

Volume of rectangular prism

$$l = 5 \text{ cm} \quad w = 5 \text{ cm} \quad h = 9 \text{ cm}$$

Volume of rectangular prism = lwh

$$= 5 \times 5 \times 9 \text{ --} [0.5]$$

$$= 225 \text{ cm}^3 \text{ --} [0.5]$$

Sangay would buy the can juice as it contains more juice.-----[1]

- c) Jamphel wants to fence his rectangular garden. He has fencing material just enough to cover 144 m^2 of the garden. If he wants the length to be 10 m longer than its width, what would be the dimensions of the garden? [3]

Answer:

$$\left. \begin{array}{l} \text{Let the width be } x \\ \text{Length} = (10 + x) \\ \text{Area} = 144 \text{ m}^2 \end{array} \right\} [0.5]$$

$x(10+x) = 144$ $10x + x^2 = 144$ -----[0.5] $x^2 + 10x - 144 = 0$ $a = 1 \quad b = 10 \quad c = -144$ $s = 10$ $P = -144$ -----[0.5] $(-8 \text{ and } 18)$ $x^2 - 8x + 18x - 144 = 0$ -----[0.5] $x(x-8) + 18(x-8) = 0$ $(x-8)(x+18) = 0$ $x = 8 \text{ or } -18$ ----- [0.5] $\therefore \text{width} = 8m$ $\text{length} = 10 + 8 = 18m$ -----[0.5]	
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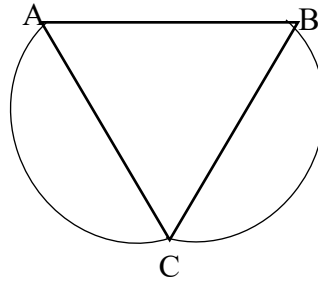
Question 3 a) <ul style="list-style-type: none"> i. Describe the transformation applied to the function $f(x) = x^2$ for the given mapping notation. $(x, y) \rightarrow \left(x + 2, -\frac{1}{5}y + 2\right)$ 	[2]
---	-----

Answer: $(x, y) \rightarrow \left(x + 2, -\frac{1}{5}y + 2\right)$ A. <i>shifted 2 units right</i> -----[0.5] B. <i>Re flected on x – axis and compressed vertically by $\frac{1}{5}$ units</i> -----[1] C. <i>shifted 2 units up</i> -----[0.5]	
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ii. Write down the final function that would result from applying the transformation for the mapping notation given in i.	[1]
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$f(x) = -\frac{1}{5}(x-2)^2 + 2$ -----[1]	
---	--

b) <ul style="list-style-type: none"> i. Create an adjacency matrix for the given digraph. 	[1.5]
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Answer: $\begin{bmatrix} 0 & 1 & 2 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{bmatrix}$ -----[1.5]

ii. Find the number of one stop-over trips between each vertices.

[1.5]

Answer: $\begin{bmatrix} 0 & 1 & 2 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{bmatrix} \times \begin{bmatrix} 0 & 1 & 2 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{bmatrix}$ -----[0.5]

$\begin{bmatrix} 0+1+4 & 0+0+4 & 0+2+0 \\ 0+0+4 & 1+0+4 & 2+0+0 \\ 0+2+0 & 2+0+0 & 4+4+0 \end{bmatrix}$ -----[0.5]

$\begin{bmatrix} 5 & 4 & 2 \\ 4 & 5 & 2 \\ 2 & 2 & 8 \end{bmatrix}$ -----[0.5]

c) Following are the goals scored by two football players in the past ten years.

Lionel Messi	73	60	58	54	53	51	61	45	41	41
Cristiano Ronaldo	42	23	42	26	33	42	60	55	51	61

i. Create a double stem and leaf plot for the data.

[2]

Answer:

Lionel Messi	41	41	45	51	53	54	58	60	61	73
Cristiano Ronaldo	23	26	33	42	42	42	51	55	60	61

Lionel Messi	Stem	Cristiano Ronaldo
	2	3 6
	3	3
5 1 1	4	2 2 2
8 4 3 1	5	1 5
1 0	6	0 1
3	7	

-----[2]

ii. What are the modes of the two sets of data?

[1]

Answer

Lionel Messi : 41 -----[0.5]

Cristiano Ronaldo : 42 -----[0.5]

iii. Calculate the ranges of the two sets of data.

[1]

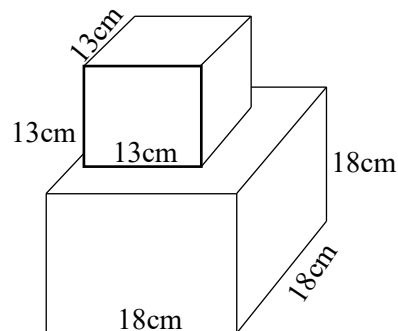
Answer

Lionel Messi : $73 - 41 = 32$ -----[0.5]

Christiano Ronaldo : $61 - 23 = 38$ -----[0.5]

Question 4

a) Deki is a carpenter and wants to create and paint a unique plant-stand for an art exhibition. Calculate the surface area of the plant-stand she will have to paint excluding the base.



[3]

Answer:

Surface area of smaller cube

$$A. \text{ of 1 face} = 13^2 = 169 \text{ cm}^2 \text{ -----[0.5]}$$

$$S.A_{\text{small cube}} = 5 \times 169 = 845 \text{ cm}^2 \text{ -----[0.5]}$$

S.A of larger cube

$$A. \text{ of 1 face} = 18 \times 18 = 324 \text{ cm}^2 \text{ -----[0.5]}$$

$$S.A_{\text{large cube}} = 4 \times 324 = 1296 \text{ cm}^2 \text{ -----[0.5]}$$

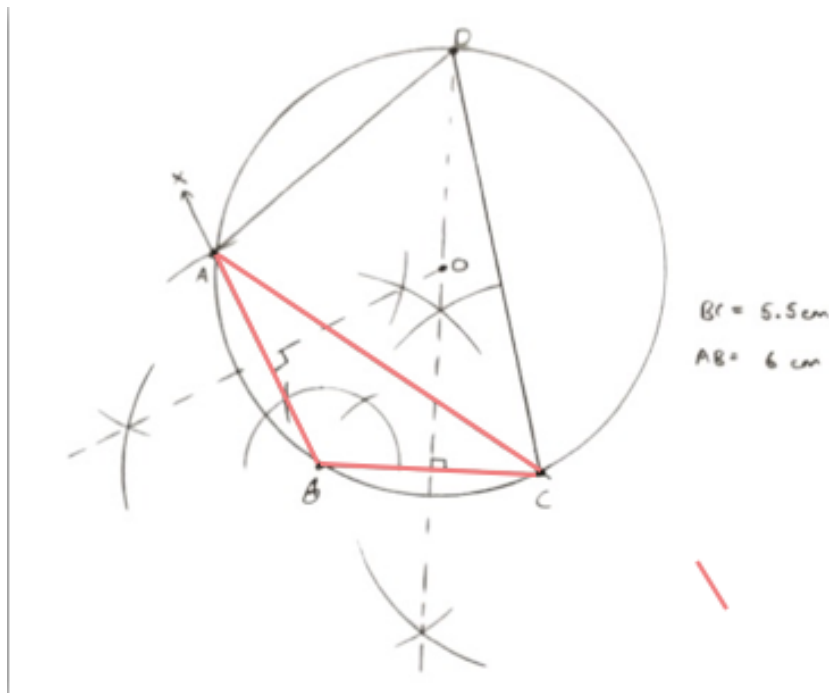
$$A. \text{ of top of large cube} = 18^2 - 13^2 = 155 \text{ cm}^2 \text{ -----[0.5]}$$

$$\begin{aligned} \text{Total surface area required to paint} &= 845 \text{ cm}^2 + 1296 \text{ cm}^2 + 155 \text{ cm}^2 \\ &= 2296 \text{ cm}^2 \text{ -----[0.5]} \end{aligned}$$

- b) Construct $\triangle ABC$ with $BC = 5.5 \text{ cm}$, $AB = 6 \text{ cm}$ and $\angle ABC = 120^\circ$. Construct circumcircle of the triangle. [4]

Answer: Triangle constructed correctly -----[2]

Circumcircle constructed correctly -----[2]



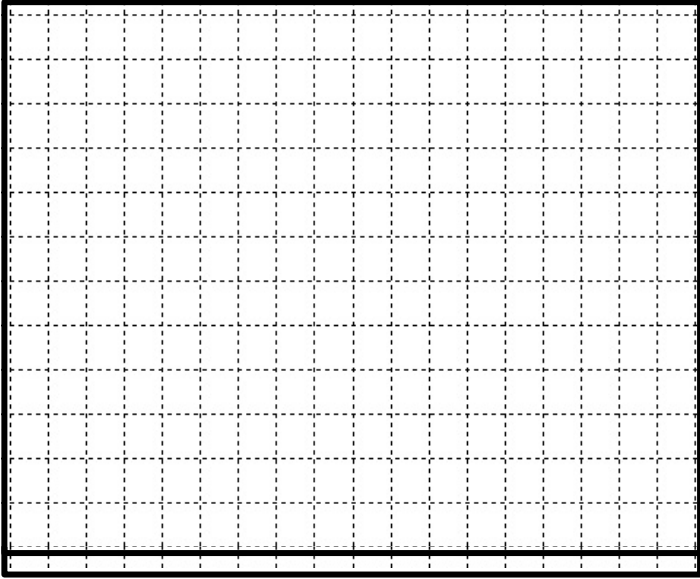
- c) A plumber charges Nu 500 for a service call and an additional charge of Nu 150 per hour.
i. Write an equation to show the relation between number of hours and total income. [1]

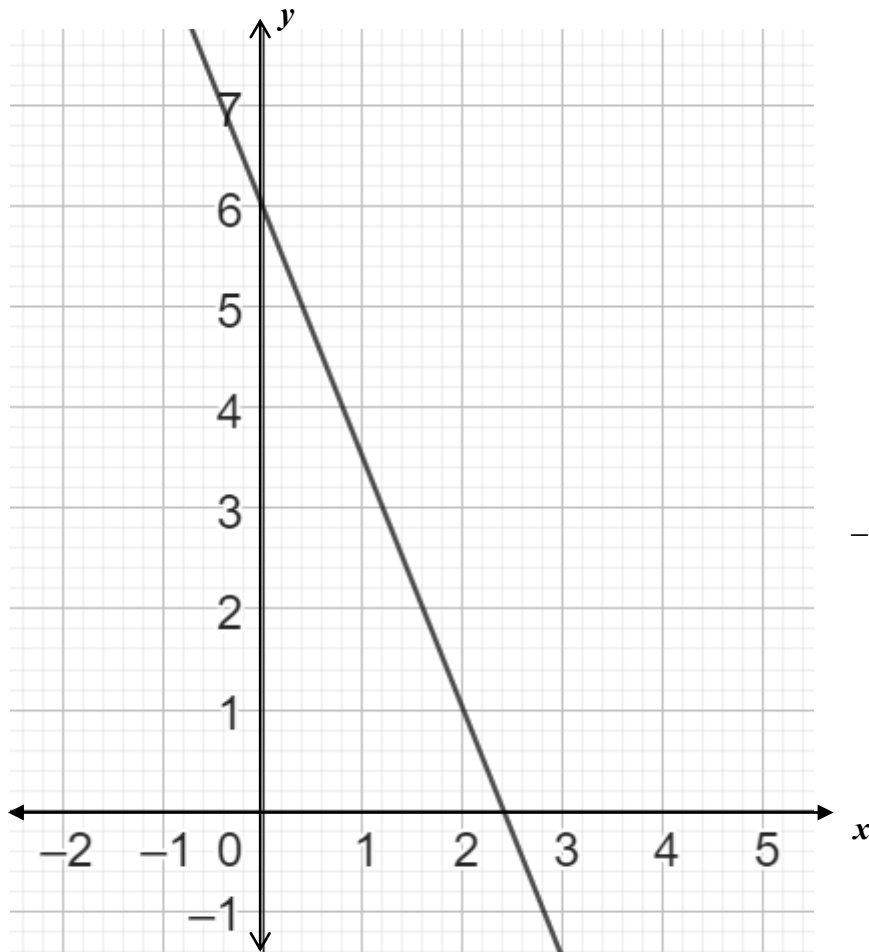
let the number of hours be x and total cost be y -----[0.5]

$$y = 150x + 500 \text{ -----[0.5]}$$

ii. How much will the plumber earn if he works for 8 hours?	[2]
$x = 8 \text{ hours}$ $y = 150(8) + 500$ -----[1] $y = 1200 + 500$ -----[0.5] $y = 1700$ -----[0.5] Therefore the plumber will earn Nu 1700.	
Question 5	
a) Each letter of a word is written on a tiles as shown, and placed in a bag. <div style="display: flex; justify-content: center; gap: 10px; margin: 10px 0;"> <div style="border: 1px solid black; padding: 5px; width: 30px; text-align: center;">P</div> <div style="border: 1px solid black; padding: 5px; width: 30px; text-align: center;">O</div> <div style="border: 1px solid black; padding: 5px; width: 30px; text-align: center;">S</div> <div style="border: 1px solid black; padding: 5px; width: 30px; text-align: center;">S</div> <div style="border: 1px solid black; padding: 5px; width: 30px; text-align: center;">I</div> <div style="border: 1px solid black; padding: 5px; width: 30px; text-align: center;">B</div> <div style="border: 1px solid black; padding: 5px; width: 30px; text-align: center;">L</div> <div style="border: 1px solid black; padding: 5px; width: 30px; text-align: center;">E</div> </div>	
i. If you drew a vowel and replaced it, what is the probability of drawing a vowel next?	[1]
Answer: $P(E) = \frac{\text{Number of favourable outcomes}}{\text{Number of theoretical outcomes}}$ $P(\text{vowel}) = \frac{3}{8}$ -----[1]	
ii. If you drew a vowel and did not replace it, what is the probability of drawing a vowel next?	[1]
Answer: $P(E) = \frac{\text{Number of favourable outcomes}}{\text{Number of theoretical outcomes}}$ $P(\text{vowel}) = \frac{2}{7}$ -----[1]	
b) Kuensang took a test in English and Mathematics. The probability of him passing in both the test is 0.6 . The probability of him passing in English test is 0.8 .What is the probability of him passing in Mathematics given that he has passed in English?	[2]
Answer: $P(\text{passing English}) = 0.8$ -----[0.5] $P(\text{passing English and Mathematics}) = 0.6$ -----[0.5] Probability of passing Mathematics given passed in English	[2]

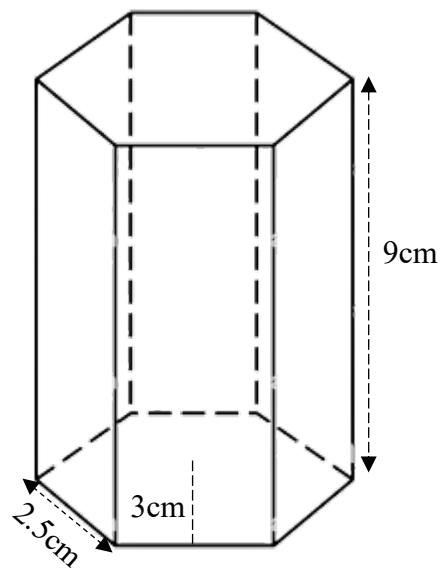
$P(M/E) = \frac{P(M \cap E)}{P(E)}$ $= \frac{0.6}{0.8} = \frac{6}{8} = \frac{3}{4} \text{ ----- [1]}$	
<p>c) Convert the following radical expressions as entire radical and arrange them from the least to the greatest.</p> $3\sqrt{5} \quad 5\sqrt{2} \quad 13 \quad 2\sqrt{3}$	[3]
<p>Answer:</p> $\sqrt{45} \quad \sqrt{50} \quad \sqrt{169} \quad \sqrt{12} \text{ ----- [0.5 \times 4]}$ $2\sqrt{3}, 3\sqrt{5}, 5\sqrt{2}, 13 \text{ ----- [1]}$	
<p>d) Prove that :</p>	
<p>i. $\sec \theta \cot \theta = \operatorname{cosec} \theta$</p>	[1]
$\sec \theta \cot \theta = \operatorname{cosec} \theta$ <p><i>LHS</i></p> $\frac{1}{\cos \theta} \times \frac{\cos \theta}{\sin \theta} = \frac{1}{\sin \theta} \text{ ----- [0.5]}$ $\therefore \frac{1}{\sin \theta} = \operatorname{cosec} \theta, \text{ hence proved ----- [0.5]}$	
<p>ii. $\frac{1 + \cos \theta - \sin^2 \theta}{\sin \theta (1 + \cos \theta)} = \cot \theta$</p>	[2]
$\frac{1 + \cos \theta - \sin^2 \theta}{\sin \theta (1 + \cos \theta)} = \cot \theta$ <p><i>LHS</i></p> $\frac{1 + \cos \theta - (1 - \cos^2 \theta)}{\sin \theta (1 + \cos \theta)}$ $= \frac{1 + \cos \theta - 1 + \cos^2 \theta}{\sin \theta (1 + \cos \theta)} \text{ ----- [0.5]}$ $= \frac{\cos \theta + \cos^2 \theta}{\sin \theta (1 + \cos \theta)} \text{ ----- [0.5]}$ $= \frac{\cos \theta (1 + \cos \theta)}{\sin \theta (1 + \cos \theta)} = \frac{\cos \theta}{\sin \theta} \text{ ----- [0.5]}$ <p>Therefore $\frac{\cos \theta}{\sin \theta} = \cot \theta, \text{ hence proved ----- [0.5]}$</p>	

Question 6	
<p>a)</p> <p>i. Convert $5x+2y=12$ into slope and y- intercept form.</p>	[1]
$5x+2y=12$ $2y=12-5x\text{---}[0.5]$ $y=\frac{12-5x}{2}$ $y=-\frac{5}{2}x+6\text{---}[0.5]$	
<p>ii. Sketch the graph of the resulting equation.</p>	[2]
	
Answer:	



---[2]

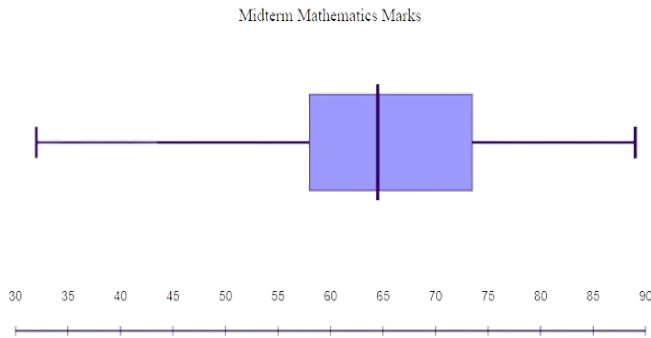
- b) Tashi, who works as a manager in CSI has created a container for packaging coffee beans grown in Bhutan as shown below.



<p>i. If the cost of printing a label is Nu 0.25 per cm^2, what would be the cost of printing a label to cover the entire lateral face of the container?</p>	[2]
<p>Answer: $Area\ of\ the\ lateral\ face = 6(9 \times 2.5) = 135\ cm^2$ ----[1] $Cost\ of\ printing = 135 \times 0.25 = Nu\ 33.75$ -----[1]</p>	
<p>ii. What is the maximum volume of coffee beans it can hold?</p>	[2]
<p>Answer: $Volume = A_{base} \times h$ $Area\ of\ base = 6\left(\frac{2.5 \times 3}{2}\right) = 22.5\ cm^2$ ----[1] $Volume = 22.5 \times 9 = 202.5\ cm^3$ -----[1] Therefore the maximum volume of coffee beans it can hold can be $202.5\ cm^3$</p>	
<p>c) Punjab National Bank declared 15% dividend rate on its stock this year. Karma owns 150 shares, each with a face value of Nu 100.</p>	
<p>i. What dividend amount did Karma receive?</p>	[1]
<p>Answer: Given $Dividend\ rate = 15\%$ $n = 150$ $fv = 100$ $Dividend\ amount = 0.15 \times 150 \times 100 = Nu\ 2,250$ -----[1]</p>	
<p>ii. If he had bought the shares at a premium of 25%, what is the yield percentage?</p>	[1]
<p>Answer: Given $Premium\ \% = 25\%$ $fv = Nu\ 100$ $MP\ of\ one\ share = 100 + 0.25 \times 100 = Nu\ 125$ $MP\ of\ 150\ shares = 125 \times 150 = Nu\ 18,750$ ----[0.5] $Yield\ \% = \frac{2,250}{18,750} = 0.12 = 12\%$ -----[0.5]</p>	
<p>iii. Would he have benefited more by investing his money in a saving account that offered 7.25% simple interest? Explain.</p>	[1]
<p>Answer: Karma would have benefited more by investing his money in buying shares as he would earn more in dividend than from saving.-----[1]</p>	

Question 7

a) The following box and whisker plot shows the Mathematics marks of midterm examination of 20 students.



i. Identify the type of data distribution.

[1]

Answer: Close to Normal distribution/ Positive right Skewed.

ii. What was the median mark?

[1]

Answer: 64 to 65

iii. Write down any **TWO** observations from the given box and whisker plot.

[2]

Sample Answer:

- The highest math marks was about 90.
- The lowest math mark was about 30.
- 50% of the students scored between 57 and 74.
- 75% of the students scored above 57.
- 25% of the students scored below 56.

b) In a test, marks were awarded for the correct answers and deducted for the incorrect answers. Mipham received 40 points by answering 12 questions correctly and 8 questions incorrectly. Neeshar received 60 points by answering 16 questions questions correctly and 4 questions incorrectly. How many points were deducted for each incorrect answer?

[3]

Let the points awarded for correct answer by x and points deducted for incorrect questions be y .

$$12x - 8y = 40 \text{ --- (eq 1)}$$

$$16x - 4y = 60 \text{ --- (eq 2)}$$

Multiplying (eq 2) by 2

$$32x - 8y = 120 \text{ --- (eq 3)}$$

Subtracting (eq1) from (eq3)

$$-20x = -80$$

$$x = \frac{-80}{-20} = 4$$

Substituting $x = 4$ in (eq1)

$$12(4) - 8y = 40$$

$$48 - 8y = 40$$

$$-8y = 40 - 48$$

$$-8y = -8$$

$$y = \frac{-8}{-8} = 1$$

Therefore 1 point was deducted for each incorrect answer.

c) Find the missing value.

i. $1 + \sqrt{2m+3} = 6$

[1.5]

Answer

$$1 + \sqrt{2m+3} = 6$$

$$\sqrt{2m+3} = 6 - 1$$

$$\sqrt{2m+3} = 5 \text{ ----- [0.5]}$$

Squaring on both sides

$$(\sqrt{2m+3})^2 = 5^2$$

$$2m + 3 = 25 \text{ ----- [0.5]}$$

$$2m = 25 - 3$$

$$m = \frac{22}{2}$$

$$m = 11 \text{ ----- [0.5]}$$

ii. $\sqrt{36x^a} \times \sqrt{48} = 24x^7 \sqrt{3x}$

[1.5]

Answer

$$\sqrt{36x^a} \times \sqrt{48} = 24x^7 \sqrt{3x}$$

$$\sqrt{36 \times 48x^a} = 24x^7 \sqrt{3x}$$

$$\sqrt{1,728x^a} = 24x^7 \sqrt{3x} \text{ -----}[0.5]$$

Squaring both sides

$$\left(\sqrt{1,728x^a}\right)^2 = \left(24x^7 \sqrt{3x}\right)^2$$

$$1,728x^a = 576x^{14} \times 3x \text{ -----}[0.5]$$

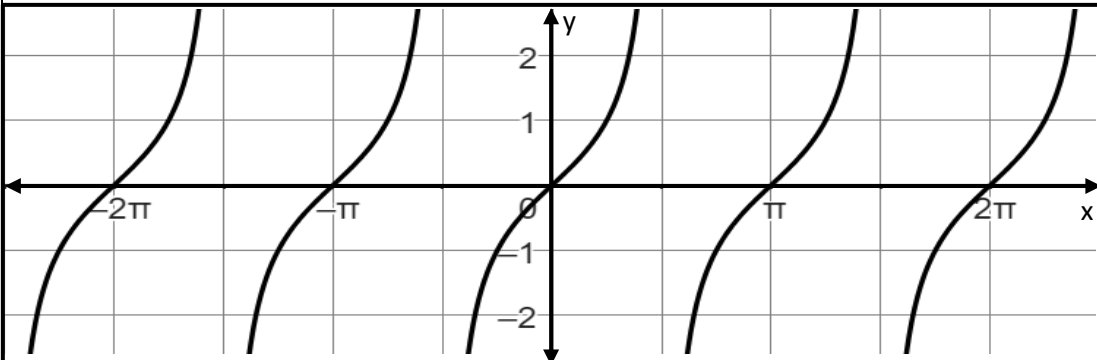
$$1,728x^a = 1728x^{15}$$

$$\therefore a = 15 \text{ -----}[0.5]$$

Question 8

a) Identify the following graphs of trigonometric functions.

i.

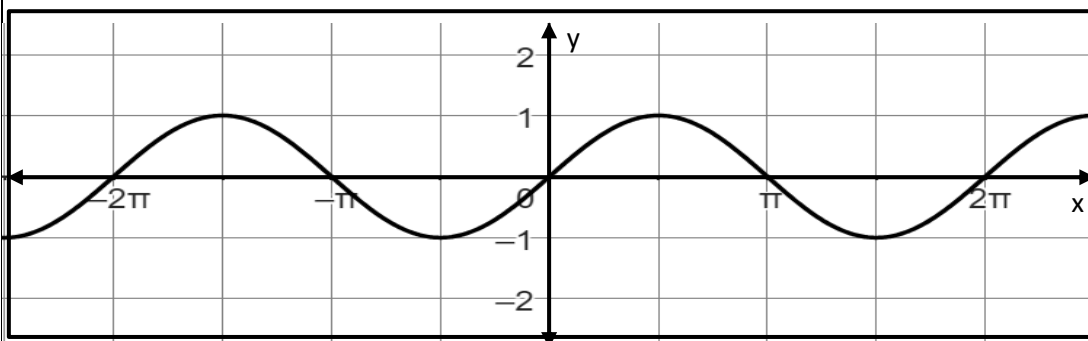


1

Answer:

Graph of $\tan(x)$

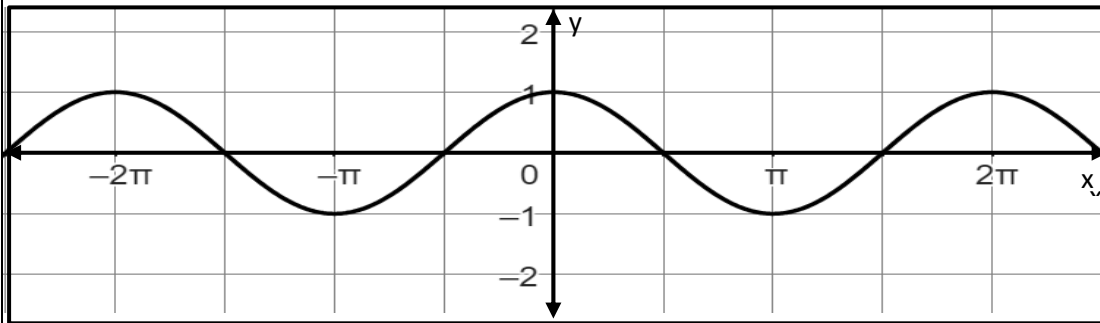
ii.



1

Answer: Graph of $\sin(x)$

iii.



1

Answer: Graph of $\cos(x)$

- b) Darshan purchased a gift for his sister and wants to wrap it in a rectangular prism box. The box has a volume of 729 cm^3 . What is the least amount of gift wrapper required to wrap the box?

[3]

Answer

Given

Volume of a cube = 729 cm^3 -----[0.5]

$s^3 = 729$ -----[0.5]

$s = \sqrt[3]{729} = 9 \text{ cm}$ -----[0.5]

Total surface area of the cube = $6s^2$

$6 \times (9)^2 = 486 \text{ cm}^2$ ----[1.5]

Therefore the least amount of gift wrapper required = 486 cm^2

- c) Tsheten sells 50 cucumbers per day at a price of Nu 20 per cucumber. She expects that for every increase in price of cucumber by Nu 1, her daily sale will decrease by 1.

- i. Create a function that represents her total sale based on the number and price increase of Nu 1.

[1]

Answer

Let the number of price increase be x .

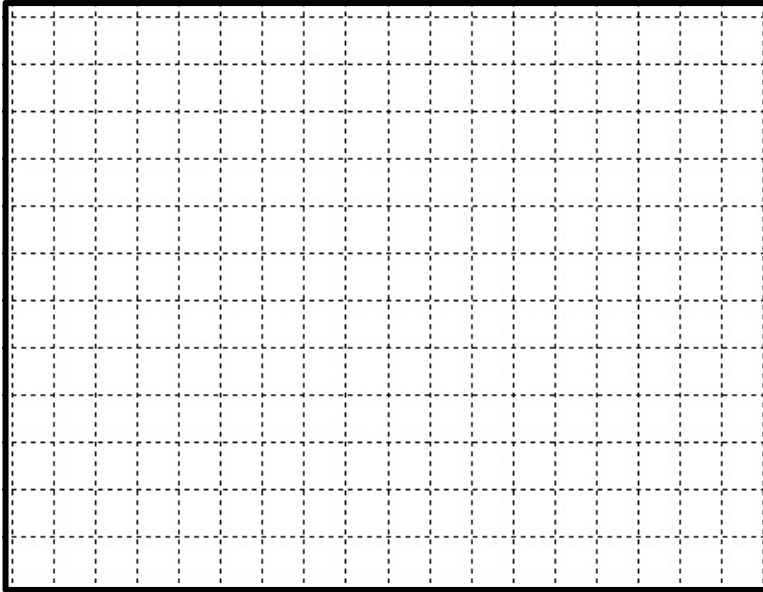
New Price = $(20 + x)$

New Sale = $(50 - x)$ -----[0.5]

Total Sale = $(20 + x)(50 - x)$

$f(x) = (20 + x)(50 - x)$ -----[0.5]

ii. Sketch the graph of function.



[3]

$$f(x) = (20+x)(50-x)$$

x-intercepts

$$y = 0$$

$$0 = (20+x)(50-x) \text{-----}[0.5]$$

$$x = -20 \text{ or } 50$$

y-intercept

$$x = 0$$

$$f(0) = (20+0)(50-0) \text{-----}[0.5]$$
$$= 1000$$

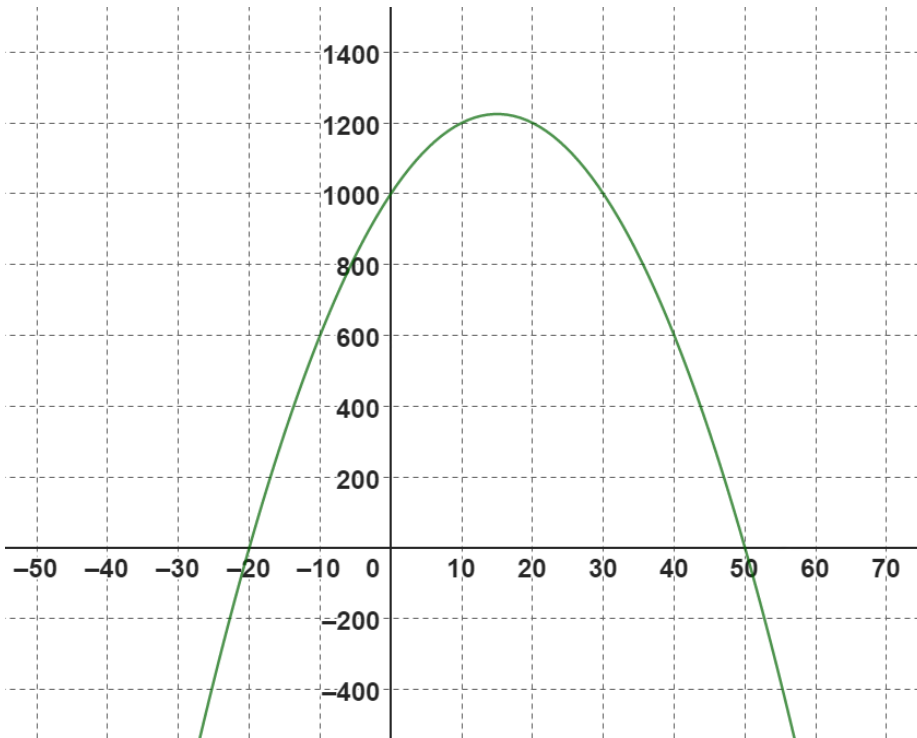
Coordinate of vertex

$$x\text{-coordinate} = \frac{-20+50}{2} = 15 \text{----}[0.5]$$

y-coordinate =

$$f(15) = (20+15)(50-15) \text{-----}[0.5]$$
$$= 1225$$

Graph-----[1]



Question 9

a) A BDBL offers a loan with a choice of two rates

- 14.7% p.a compounded monthly.
- 15% p.a compounded semi annually.

Which rate would you choice? Why?

[3]

Answer:

rate at 14.7%

$$r = 0.147$$

$$n = 12$$

$$\left. \begin{aligned} \text{Effective annual rate} &= \left(1 + \frac{r}{n}\right)^n - 1 \\ &= \left(1 + \frac{0.147}{12}\right)^{12} - 1 \\ \text{EAR} &= 0.154 \end{aligned} \right\} \dots\dots\dots [1]$$

rate at 15.0%

$$r = 0.15$$

$$n = 2$$

$$\left. \begin{aligned} \text{Effective annual rate} &= \left(1 + \frac{r}{n}\right)^n - 1 \\ &= \left(1 + \frac{0.15}{2}\right)^2 - 1 \\ \text{EAR} &= 0.14 \end{aligned} \right\} \dots\dots\dots [1]$$

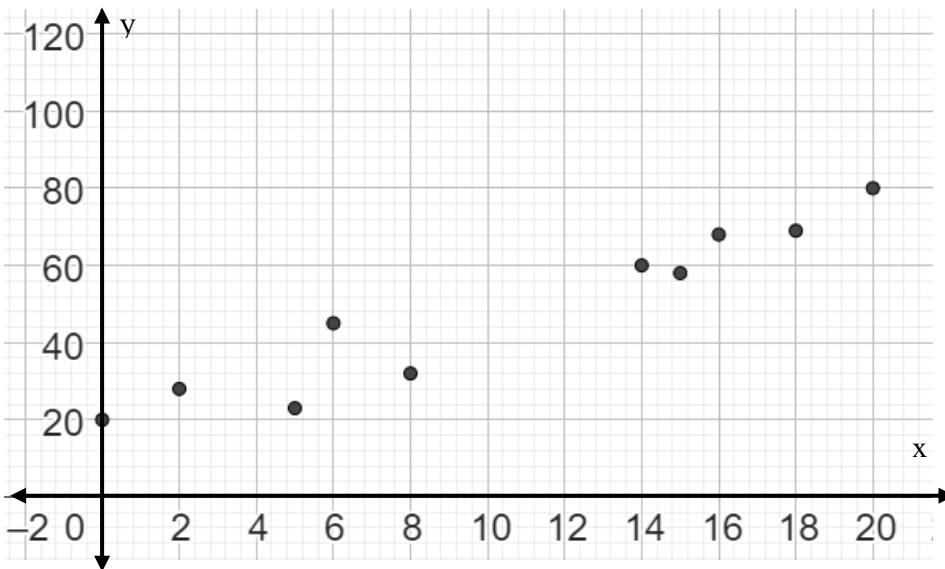
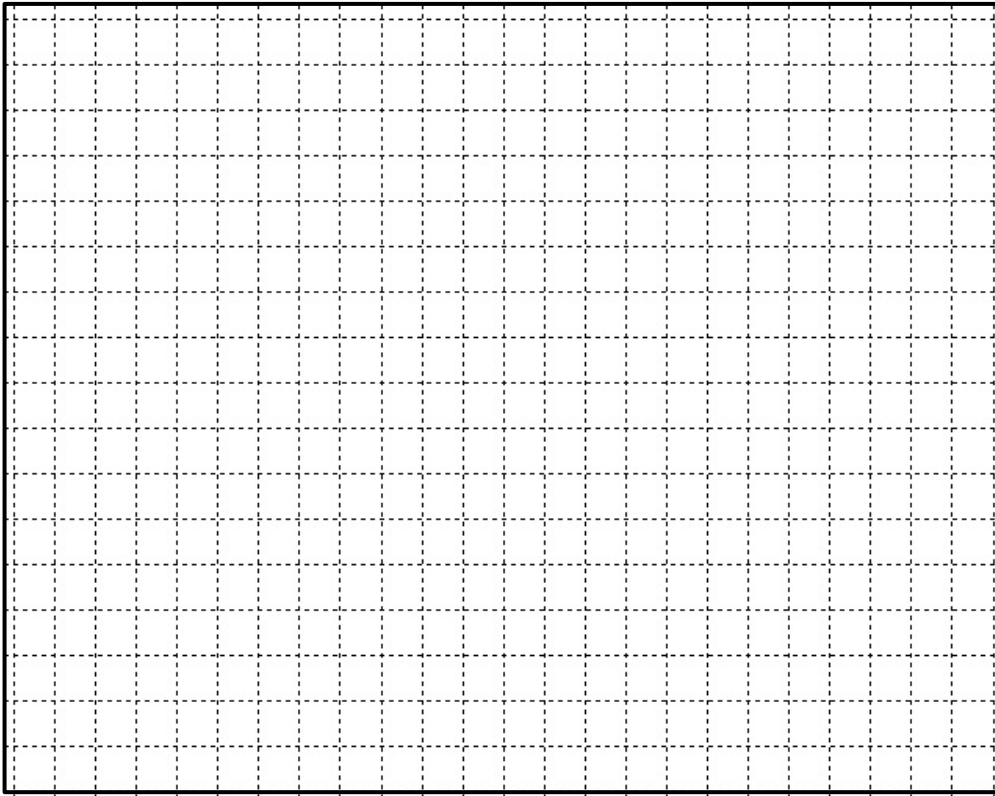
I will choice option with rate 15 % as effective annual rate is lower . -----[1].

b) The table below shows the amount of time a group of students spent revising for the end of year exam and the scores they achieved in the exam.

Hours of revision	0	2	5	6	8	10	13	14	15	16	18	25
Exam Score	20	28	23	45	32	63	52	60	58	68	69	80

i. Draw a scatter plot to represent the above information.

[2]



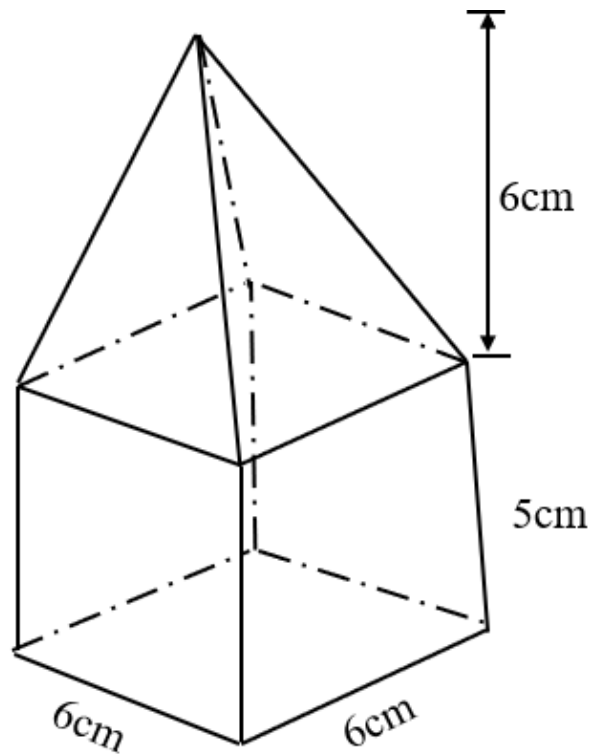
ii. Describe the relationship between the time spent revising and the score achieved in the exam.

[1]

Sample Answer:

The more number of hours the students spent in preparing for exam the marks scored is also higher.

c) For the composite shape given below:



Calculate the volume

[2]

Answer

$$\text{Volume of pyramid} = \frac{1}{3}(6^2 \times 6) = 72\text{cm}^3 \text{ -----}[1]$$

$$\text{Volume of cuboid} = 6\text{cm} \times 6\text{cm} \times 5\text{cm} = 180\text{cm}^3 \text{ -----}[0.5]$$

$$\text{Total volume} = 72\text{cm}^3 + 180\text{cm}^3 = 252\text{cm}^3 \text{ -----}[0.5]$$

d) Solve the system of linear equation

$$2x + 3y = 6$$

$$4x - y = 5$$

[2]

Answer.

$$2x + 3y = 6 \dots \dots \dots \text{eqn 1}$$

$$4x - y = 5 \dots \dots \dots \text{eqn 2}$$

$$\left. \begin{array}{l} -y = 5 - 4x \\ y = 4x - 5 \end{array} \right\} \dots \dots \dots [0.5]$$

sub.in eqn 1

$$2x + 3(4x - 5) = 6$$

$$2x + 12x - 15 = 6$$

$$14x = 21$$

$$x = \frac{21}{14}$$

$$x = \frac{3}{2} \dots \dots \dots [0.5]$$

$$4 \times \frac{3}{2} - y = 5$$

$$6 - y = 5$$

$$y = 1 \dots \dots \dots [0.5]$$